

ELECTRIC FIELD

An alternative method of describing the interaction between charges is to introduce the concept of the electric field E . Recall in our brief overview of Maxwell's equations that we mentioned that the E -field is a fundamental quantity in Maxwell's equations that is very important in understanding E&M.

Def: The Electric Field E at a point in space is equal to the electric force F that a test charge q_0 experiences, divided by the test charge q_0 .

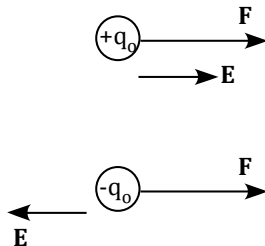
$$\boxed{\vec{E} = \frac{\vec{F}}{q_0}} \text{ Electric Field}$$

Units

$$[E] = \text{N/C}$$

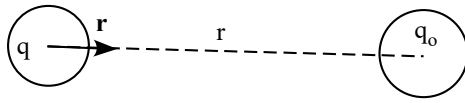
The test charge q_0 can be positive or negative:

- If q_0 is positive, \mathbf{F} and \mathbf{E} are in same direction.
- If q_0 is negative, \mathbf{F} and \mathbf{E} are in opposite direction.



- One of the reasons the E -field concept is very important is because it allows us to calculate the force \mathbf{F} that a charge q will experience if we know the E -field.
- If a charge q is placed at a point where the E -field is \mathbf{E} , then it will experience an electric force $\mathbf{F} = q\mathbf{E}$.

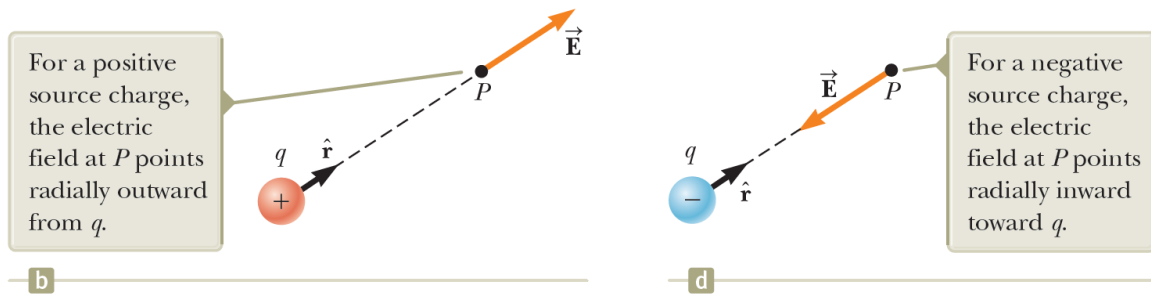
Ex. Calculate the E-field at a distance r from a point charge q.



$$\vec{F} = \frac{kq q_0}{r^2} \hat{r}$$

$$\vec{E} = \frac{\vec{F}}{q_0} = \frac{kq}{r^2} \hat{r} \quad \text{Electric Field due to a point charge.}$$

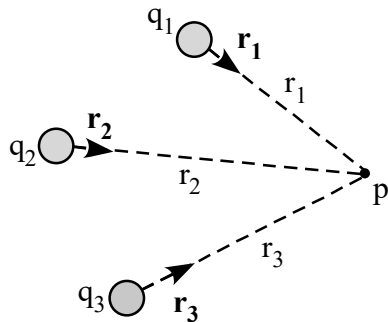
- a) If q is positive, then the E-field is symmetrically radially outward.
- b) If q is negative, then the E-field is symmetrically radially inward.
- c) The electric field is a property of the charge q and is independent of the test charge q₀



One of the reasons the **E**-field concept is very important is because it allows us to calculate the force **F** that a charge q will experience if we know the E-field. The force is given by $\mathbf{F} = q\mathbf{E}$.

Superposition Principle for E-Fields

The Electric Field at some point in space is equal to the sum of the Electric Fields due to the surrounding charges.



$$\vec{E} = \vec{E}_1 + \vec{E}_2 + \vec{E}_3$$

$$\vec{E} = \frac{kq_1}{r_1^2} \hat{r}_1 + \frac{kq_2}{r_2^2} \hat{r}_2 + \frac{kq_3}{r_3^2} \hat{r}_3$$

In general, for n – point charges:

$$\boxed{\vec{E} = k \sum \frac{q_n \hat{r}_n}{r_n^2}} \text{ E-field due to n-point charges.}$$

If you know the E-field at any point in space, you can determine the force on a charge q placed at that point by $\mathbf{F} = q\mathbf{E}$. Using the E-field concept we say that it's the E-field that exerts the force F on q .